

Higher-order readings of WH-questions

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The traditional view

WH-questions expect answers naming an **entity** in the extension of the WH-complement or a **generalized quantifier** (GQ) over a set of such entities.

(1) Which student came?

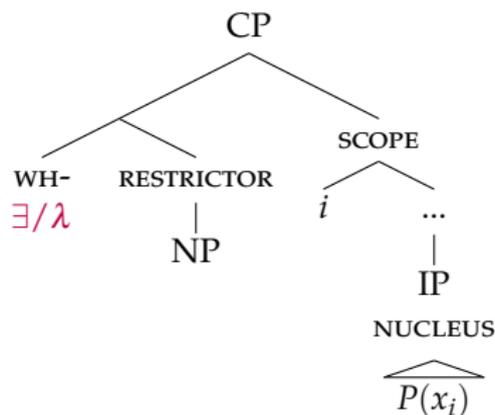
a. Andy.

\rightsquigarrow *Andy is a student.*

b. Andy or Billy.

\rightsquigarrow *Andy and Billy are students.*

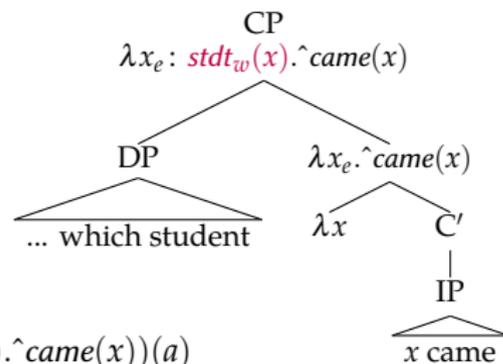
A general solution: The WH-phrase is a **binders of e -type variables**.



The traditional view: In categorial approaches ...

WH-phrases are **function domain restrictors**. A WH-question denotes a **Q-function** only defined for meanings in $\llbracket \text{WH-complement} \rrbracket$.

(2) Which student came?



a. **Entity**-naming answers

$$\begin{aligned} \llbracket \text{WH-Q} \rrbracket (\llbracket \text{Andy} \rrbracket) &= (\lambda x_e: \text{stdt}_w(x). \hat{\text{came}}(x))(a) \\ &= \text{stdt}_w(a). \hat{\text{came}}(a) \end{aligned}$$

b. **GQ**-naming answers

$$\begin{aligned} \llbracket \text{Andy or Billy} \rrbracket (\llbracket \text{WH-Q} \rrbracket) &= (a^\uparrow \sqcup b^\uparrow) (\lambda x_e: \text{stdt}_w(x). \hat{\text{came}}(x)) \\ &= \text{stdt}_w(a) \wedge \text{stdt}_w(b). \hat{\text{came}}(a) \cup \hat{\text{came}}(b) \end{aligned}$$

In short: **Q-domain** \subseteq $\llbracket \text{WH-complement} \rrbracket$

[Q-domain = Dom(Q-function). In other approaches, Q-domain refers to the set of values that a WH-bound variable can take.]

My claim

Some WH-questions admit **higher-order readings**, under which the Q-domain ranges over a set of higher-order meanings. Thus, *wh*-phrases can also bind higher-order variables.

Roadmap

- A. Evidence for a higher-order Q-domain
- B. Defining a higher-order Q-domain: The Positiveness Constraint
- C. Distributing and deriving higher-order readings
- D. Appendix: The 'disjunction-only' higher-order reading

A. Evidence for a higher-order Q-domain

If Q-domain \subseteq WH-complement

For any answer naming a GQ ...

- 1 this GQ must be interpreted with **wide scope** relative to the Q-nucleus.
- 2 this answer is not in the Hamblin-set — its derivation involves extra Boolean operations to the propositions in the Hamblin-set.

- **Non-reducibility**: diagnostic for disjunctions and \exists -GQs
- **Stubborn collectivity**: diagnostic for conjunctions and \forall -GQs
- Diagnostics for GQ-coordinations

1. Non-reducibility: Diagnostic for disjunctions

Spector (2007, 2008): Elided disjunctions can completely address \square -questions.

(7) Which books does John **have to** read?

The French novels **or** the Russian novels.

a. 'F or R ... I don't know which exactly.'

Partial: $or \gg \square$

b. 'F or R ... the choice is up to him.'

Complete: $\square \gg or$

(8) a. **First-order reading:**

'Which book(s) x is s.t. J has to read x ?'
[[... which books] λx [have-to [J read x_e]]

b. **Higher-order reading:**

'What GQ π over books is s.t. J has to read π ?'
[[... which books] $\lambda \pi$ [have-to [$\pi_{\langle et,t \rangle}$ λx [J read x_e]]]]

The higher-order reading involves **semantic reconstruction** (*a la* Cresti 1995).

$$\begin{aligned} \llbracket \text{WH-Q} \rrbracket (\llbracket \text{F or R} \rrbracket) &= (\lambda \pi_{\langle et,t \rangle} : \text{SMLO}(\pi) \subseteq *book. \square [\lambda w. \pi(\lambda x. read_w(j, x))]) (f^\uparrow \sqcup r^\uparrow) \\ &= \text{SMLO}(f^\uparrow \sqcup r^\uparrow) \subseteq *book. \square [\lambda w. (f^\uparrow \sqcup r^\uparrow)(\lambda x. read_w(j, x))] \\ &= \{f, r\} \subseteq *book. \square [\lambda w. read_w(j, f) \vee read_w(j, r)] \end{aligned}$$

[NB: the Q-domain is subject to revision]

1. Non-reducibility: Diagnostic for disjunctions

The \Box -question helps to validate the existence of Boolean disjunctions in a Q-domain because its answer space is **not closed under disjunction**.

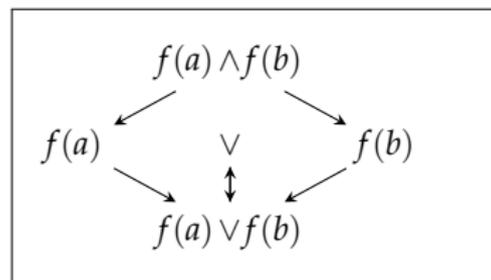


Figure 1: What did John read?

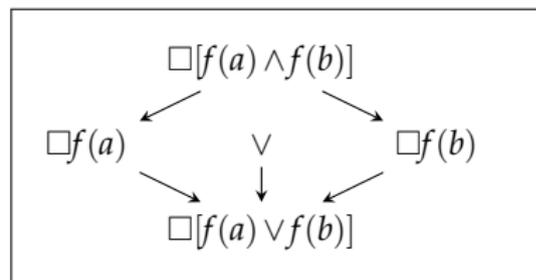


Figure 2: What does John have to read?

Or, the Q-function of the \Box -question is **not reducible** relative to disjunctions.

Reducibility relative to disjunctions

A function θ is reducible relative to disjunctions iff for any meanings a and b s.t. θ is defined for a and b or for a^\uparrow and b^\uparrow : $\theta \bullet (a^\uparrow \sqcup b^\uparrow) \equiv (\theta \bullet a^\uparrow) \sqcup (\theta \bullet b^\uparrow)$.

[\bullet : the combinatory operation between θ and a GQ]

(9) John must read a or $b \neq$ John must read a or John must read b .

1. Non-reducibility: Diagnostic for disjunctions

The diagnostic for disjunctions can be made based on any WH-questions where the Q-function is not reducible relative to disjunctions.

(10) Attitude verbs

- a. Which books did John **demand** that we read?
- b. Which books is John **certain** that Mary read?
- c. Which books does John **expect** Mary to read?

(11) Modals

- a. Which books is it **sufficient** to read?
- b. Which books is John **required** to read?

(12) Quantifiers

- a. Which books did **most/all** of the students read?
- b. Which books does John **always/ usually** read?

[(10) and (11) are from Spector (2007).]

1. Non-reducibility: Diagnostic for \exists -quantifiers

The non-reducibility diagnostic also extends to many \exists -quantifiers.

Non-reducibility test

A function θ is reducible relative to a GQ π iff $\theta \bullet \pi \equiv \pi(\lambda x. \theta \bullet x^\uparrow)$

(13) John must read $\left\{ \begin{array}{l} \text{at least} \\ \text{more than} \\ \text{exactly} \end{array} \right\}$ two books by Balzac.

\neq There are $\left\{ \begin{array}{l} \text{at least} \\ \text{more than} \\ \text{exactly} \end{array} \right\}$ two books by Balzac that John must read.

(14) Which books does John have to read?

$\left\{ \begin{array}{l} \text{At least} \\ \text{More than} \\ \text{Exactly} \end{array} \right\}$ two books by Balzac.

(${}^{\text{OK}}\exists \gg \square$, ${}^{\text{OK}}\square \gg \exists$)

2. Stubborn collectivity: Diagnostic for conjunctions

Quantized collective predicates (e.g. *formed a team*, *co-authored two papers*) are “**stubbornly collective**” (in contrast to e.g. *lifted the piano*).

Context: The kids formed two teams in total: $a + b$ formed one, $c + d$ formed one.



- (15) a. The kids **formed teams**.
b. #The kids **formed a team**.
- (16) a. #John knows [that **the kids** formed a team].
b. John knows [**which kids** formed a team].
 \rightsquigarrow John knows that $a + b$ formed a team **and** $c + d$ formed a team.

Puzzle: Where does the conjunctive closure in (16b) come from?

Clearly, it cannot come from the predicate or anywhere within the Q-nucleus.

2. Stubborn collectivity: Diagnostic for conjunctions

Proposal (Xiang 2016: §1.6)

The conjunctive closure is supplied by the **WH-phrase**: it binds a higher-order trace and yields a Q-domain which includes also **Boolean conjunctions**.

(17) Which kids formed a team?

'For which GQ π over kids is such that π formed a team?'

a. **Logical Form**

$[[\dots \text{ which kids}] \lambda \pi \dots [_{\text{IP}} \pi_{\langle et, t \rangle} \lambda x [_{\text{VP}} x_e \text{ formed a team }]]]$

b. **Q-function** (domain to be revised)

$[[_{\text{WH-Q}}] = \lambda \pi_{\langle et, t \rangle} : \text{SMLO}(\pi) \subseteq *kid. \hat{\pi}(\lambda x. \text{form-a-team}(x))$

c. **Combining with a Boolean conjunction**

$[[_{\text{WH-Q}}]((a \oplus b)^{\uparrow} \sqcap (c \oplus d)^{\uparrow})$

$= \{a \oplus b, c \oplus d\} \subseteq *kid. \lambda w [\text{form-a-team}_w(a \oplus b) \wedge \text{form-a-team}_w(c \oplus d)]$

2. Stubborn collectivity: Diagnostic for conjunctions

Another (problematic) view: The conjunctive closure is from an operation outside the Q-root, such as Heim's (1994) answerhood-operator.

$$(18) \text{ ANS-H}(Q)(w) = \bigcap \{p \mid w \in p \in Q\}$$

No. The contrast between (19a) and (19b) wrt uniqueness shows that the conjunctive closure comes from the WH-phrase.

- (19) a. John knows [which **kids** formed a team].
b. #John knows [which **two kids** formed a team].
↔ Among the relevant kids, exactly two of them formed one single team.

Dayal (1996): A question is defined only if it has a strongest true answer.

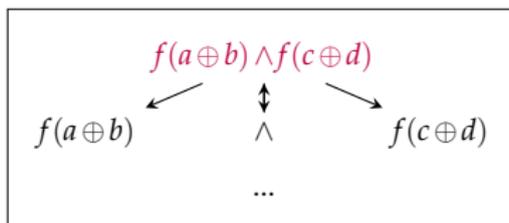


Figure 3: Which **two** kids formed a team?

The Q-domain of the basic plural-Q includes Boolean conjunctions, while that of the num-modified-Q doesn't.

3. Diagnostic for GQ-compounds

Stubborn collectivity + Non-reducibility: Disjunctions over GQs

(w: As part of the course requirement, each pair of students have to co-present one paper this or next week. Moreover, the instructor requires the presentations in each week to be given by students from the same dept.)

junior linguists:	$\{a_1, b_1\}$		junior philosophers:	$\{a_2, b_2\}$
senior linguists:	$\{c_1, d_1\}$		senior philosophers:	$\{c_2, d_2\}$

- (20) Guest: “Which students **have to present a paper together** this week?”
Instructor: “The two junior linguists and the two senior linguists, OR, the two junior philosophers and the two senior philosophers.”
($\square \gg$ or \gg and)

- (21) a. [[... which students] $\lambda \pi$ [_{IP} have to [$\pi_{(et,t)}$ λx [_{VP} x_e p.a.p.t.]]]]
b. $((a_1 \oplus b_1)^\uparrow \sqcap (c_1 \oplus d_1)^\uparrow) \sqcup ((a_2 \oplus b_2)^\uparrow \sqcap (c_2 \oplus d_2)^\uparrow)$

3. Diagnostic for GQ-compounds

Non-reducibility: Conjunctions over GQs

(*w*: Jack is tolerated of taking up to one course a year in syntax or semantics, but he would be worried that if he has to take one or more courses for each subfield.)

- (22) What courses is Jack **worried** that he **must** take [this year]?
- a. Semantics I or II, and, Syntax I or II. (*worried* \gg *and* \gg \square \gg *or*)
 - b. At least one course in semantics and at least one course in syntax.
- (23) a. [*whP* $\lambda\pi$ [*Jack*_{*i*} is worried that [must [$\pi_{\langle et,t \rangle}$ λx [*he*_{*i*} takes *x*_{*e*}]]]]]]
- b. ($sem_1^{\uparrow} \sqcup sem_2^{\uparrow}$) \sqcap ($syn_1^{\uparrow} \sqcup syn_2^{\uparrow}$)

4. Interim summary

- A WH-phrase can bind a variable with a complex type $\langle et, t \rangle$, yielding a higher-order reading.

(24) [... whP $\lambda\pi$ [_{IP} ... $\pi_{\langle et, t \rangle}$ λx [... x_e ...]]]

- A higher-order Q-domain should include at least the following:
 - Boolean disjunctions and \exists -GQs (by non-reducibility)
 - Boolean conjunctions and \forall -GQs (by stubborn collectivity)
 - Boolean coordinations of those above

Next: Can we make the following generalization?

The higher-order Q-domain yielded by a WH-phrase consists of **all** GQs over subsets of the WH-complement and the **Boolean compounds** of these GQs.

No. Higher-order Q-domains are subject to **Positiveness**.

B. Defining a higher-order Q-domain: The Positiveness Constraint

Is there any GQ(-compound) that cannot be included in a Q-domain?

The Completeness Test

(generalized from Spector 2008)

- 1 x knows $Q \rightsquigarrow x$ knows the complete true answer of Q .
- 2 For a proposition p naming a short answer x , if p is true but isn't entailed by the complete true answer of Q , then: $p \notin$ Hamblin set and $x \notin$ Q-domain.

(25) Assume that John's reading obligations include the following:

- a. John must read **at least two** novel(s) by Andy,
- b. John must read **no** book by Billy,

(26) Sue knows which books John must read.

- | | |
|---------------------------------------|---------------------------|
| \rightsquigarrow Sue knows (a). | increasing GQ |
| \nrightarrow Sue knows (b). | decreasing GQ |
| \nrightarrow Sue knows (a) and (b). | non-monotonic GQ-compound |

From increasing-ness to positive-ness

Spector: The GQ[-compound]s included in a Q-domain must be **increasing**.

- (27) Assume that John's reading obligations include the following:
- a. John must read {**at least two, more than one**} book(s) by Andy,
 - b. John must read **no** book by Billy,
 - c. John must read {**at most one, less than two**} book(s) by Cindy,
 - d. John must read {**no more than two, up to two**} books by Danny,
 - e. John must read **no** books **except *Red Linguists*** by Emmy,
 - f. John must read **no** books **except *Blue Linguists*** by Florian,
 - g. **John must read exactly two books by Gillion.**
- (28) Sue knows which books John must read.
- ↪ Sue knows **(a)** and **(e)**. increasing GQs
 - ↯ Sue knows **(b)/(c)/(d)/(f)** decreasing GQs
 - ↯ Sue knows **(a)** and **(b)/(c)/(d)/(f)** ... non-monotonic GQ-compounds
 - ↪ **Sue knows (g).** **non-monotonic GQs**

Spector can't explain the inclusion of non-monotonic GQs and the exclusion of non-monotonic GQ-compounds.

The Positiveness Constraint

My view: Whether a GQ(-compound) should be included in a higher-order Q-domain is determined by its “**positiveness**”, not its monotonicity.

The Positiveness Constraint

Only positive GQs and their coordination compounds can be in a Q-domain.

(29) A generalized quantifier π is **positive** iff $\pi \subseteq \text{some}(\text{SMLO}(\pi))$.

π	SMLO(π)	Increasing?	Positive?
a^\uparrow	$\{a\}$	Yes	Yes
$a^\uparrow \sqcap b^\uparrow, a^\uparrow \sqcup b^\uparrow$	$\{a, b\}$	Yes	Yes
at least two books	<i>books</i>	Yes	Yes
at most two books	<i>books</i>	No	No
every book except a	<i>book</i> – $\{a\}$	Yes	Yes
no book except a	<i>book</i> – $\{a\}$	No	No
exactly two books	<i>books</i>	No	Yes
two to ten books	<i>books</i>	No	Yes

Defining a higher-order Q-domain

Let A (of type $\langle e, t \rangle$) be the set denoted by the extension of the WH -complement, then the **higher-order Q-domain** yielded by $\text{WH-}A$ (if exists) is as follows:

$$(30) \quad {}^H A = \text{MIN} \left\{ A' \mid \begin{array}{l} \forall \pi_{\langle et, t \rangle} [\text{SMLO}(\pi) \subseteq A \wedge \pi \subseteq \text{some}(\text{SMLO}(\pi)) \rightarrow \pi \in A'] \\ \wedge \forall \alpha [\emptyset \subset \alpha \subseteq A' \rightarrow \sqcup \alpha \in A' \wedge \sqcap \alpha \in A'] \end{array} \right\}$$

(The minimal set which includes all the positive GQs living on a subset of A and the Boolean coordination compounds of these GQs.)

(31) Which books does John have to read?

a. **First-order reading**

$$\lambda x_e : x \in {}^* \text{book}_w. \square \lambda w. \text{read}_w(j, x)$$

b. **Higher-order reading** (narrow scope π)

$$\lambda \pi_{\langle et, t \rangle} : \pi \in {}^{H^*} \text{book}_w. \square \lambda w. \pi(\lambda x. \text{read}_w(j, x))$$

[NB: $\text{SMLO}(\pi)$ presupposes that π has a **live-on** property, and hence that π can be decomposed into a **conservative** type $\langle 1, 1 \rangle$ quantifier (i.e., a quantifier that can be lexicalized into a determiner) and a live-on set. It thus excludes many unwanted higher-order meanings.]

C. Distributing and deriving higher-order readings

Higher-order readings are unavailable if the WH-phrase ...

- ① ... is extracted out of a weak island (Spector 2008, skipped)
- ② ... is SG-marked (Fox 2013; contra Elliott et al. 2017)
- ③ ... is NUM-modified (Xiang 2016)

- Uniqueness effects show that the following questions cannot have answers naming Boolean conjunctions.

(32) I know which **book** John read,

... Book A.

#... Book A and Book B.

(33) I know which **two** kids formed a team,

... the two boys.

#... the two boys and the two girls.

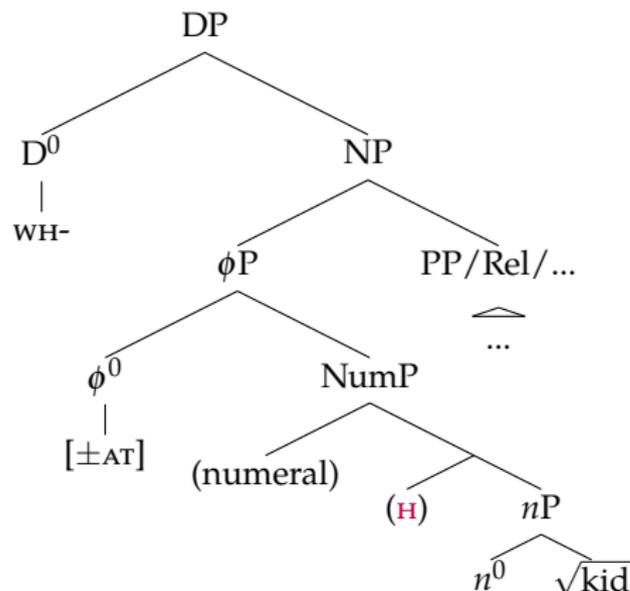
- But, unlike numeral-modifiers, PP-modifiers do not trigger uniqueness.

(34) I know which kids **in a group of two** formed a team,

... the two boys.

... the two boys and the two girls.

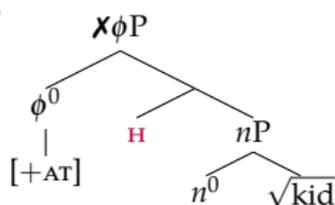
(no uniqueness)



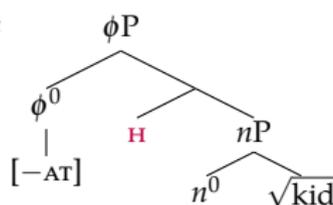
The **n-shifter** is applied to *nP*, where roots are assigned to the category of nouns and are structured into semi-lattices. [Assumptions on NP structure are from Sauerland (2003), Harbour (2014), Scontras (2014), Marti (2018). Note that a sg-marked phrase can be number-neutral in semantics (e.g., Spanish *quién* ‘who.sg’; see Maldonado (2017), Alonso-Ovalle & Rouillard (2018), cf. Elliott et al. (2017))]

1. The H-shifter cannot be used in N_{SG} : GQs are not atomic.

(35) a. *kid*

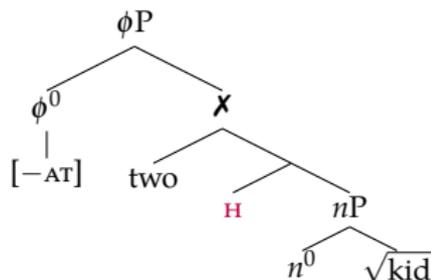


b. *kids*

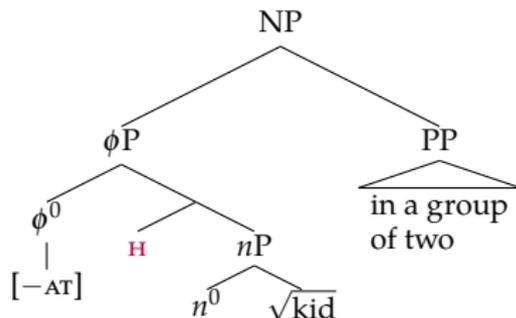


2. The H-shifter cannot be used in Num-N: numerals must check cardinality and cannot combine with a set of GQs.

(36) a. *two kids*



b. *kids in a group of two*



Conclusion

- **Evidence**

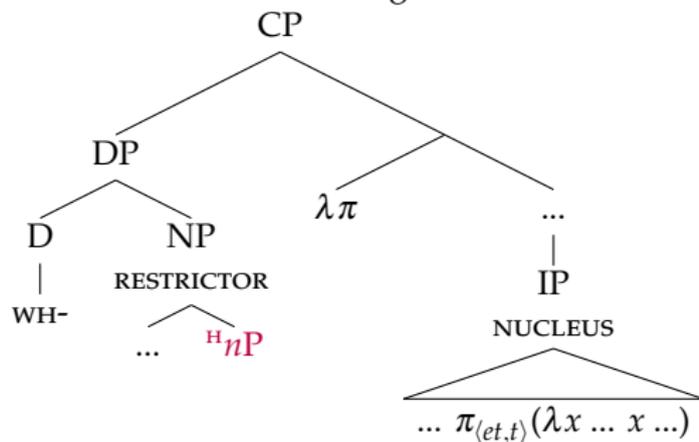
Diagnostics based on non-reducibility and stubborn collectivity show that some WH-questions admit higher-order readings.

- **The Positiveness Constraint**

A higher-order Q-domain consists of only positive GQs and their Boolean coordinations.

- **Derivation**

- A H-shifter applies to the nP within the WH-complement and returns a higher-order restrictor.
- WH-movement leaves a higher-order trace in the question nucleus.



Appendix. The 'disjunction-only' higher-order reading

A caveat about disjunctive answers: □-questions

In responding to □-questions where the WH-phrase is SG-marked or NUM-modified, narrow scope disjunctions are not as bad as conjunctions.

(37) I know which **book** John has to read,

#... Book A and Book B.

?... Book A or Book B.

(*or* ≫ □, ?□ ≫ *or*)

(38) I know which **two** books John has to read ...

#... the two French books and the two Russian books.

?... the two French books or the two Russian books. (*or* ≫ □, ?□ ≫ *or*)

Narrow scope readings of disjunctions are more readily available in proper contexts:

(39) Which textbook should we use for this class?

Heim&Kratzer or *Meaning&Grammar*, (the choice is up to you.)

A caveat about disjunctive answers: \diamond /MS-questions

Elided mention-all (MA-)answers of \diamond -questions can have a conjunctive form or a disjunctive form. (See Xiang (2016: ch. 2) for derivations.)

- (40) a. What can I use for this class?
b. Heim&Kratzer **or**/**and** *Meaning and Grammar*.
'You can use H&K and you can use M&G.'

A sg-marked \diamond -question admits a multi-choice reading if the uniqueness inference evoked by the sg-WHP takes narrow scope. (Hirsch & Schwarz 2019)

- (41) a. Which letter could be missing in *fo__m*?
b. The missing letter could be *a* and the missing letter could be *r*.

But, elided MA-answers of sg-marked \diamond -questions must be disjunctions.

- (42) a. Which textbook can I use for this class?
b. Heim&Kratzer **or**/**#and** *Meaning and Grammar*.
- (43) a. Which letter could be missing in *fo__m*?
b. Letter *a* **or**/**#and** letter *r*

Puzzles:

- 1 why these marked \square/\diamond -questions admit only disjunctions?
- 2 why this 'disjunction-only' reading is available even if the WH-P is SG-marked or NUM-modified?

Proposal: The 'disjunction-only' reading involves **reconstructing** the WH-complement to the question nucleus.

(44) Which book does John have to read?

a. First-order + reconstruction

(i) $[\text{CP which}_D \lambda x \dots \square [x \text{ is the book that J read}]]$

(ii) $\lambda x_e : x \in D. \square \lambda w [x = \iota y [\text{book}_w(y) \wedge \text{read}_w(y)]]$

b. Higher-order + reconstruction

(i) $[\text{CP which}_H \lambda \pi \dots \square [\pi_{\langle et, t \rangle} \lambda x. x_e \text{ is the book that J read}]]$

(ii) $\lambda \pi_{\langle et, t \rangle} : \pi \in {}^H D. \square \lambda w [\pi(\lambda x_e. x = \iota y [\text{book}_w(y) \wedge \text{read}_w(j, y)])]$

The H-shifter can be applied since the discourse domain D is unmarked.

Conjunctive answers are unacceptable because they yield a contradiction.

(45) Which book does John have to read?

$$\llbracket \text{CP} \rrbracket = \lambda \pi_{\langle et, t \rangle} : \pi \in {}^H D. \square \lambda w [\pi (\lambda x_e . x = \iota y [\text{book}_w(y) \wedge \text{read}_w(j, y)])]$$

a. Book A or Book B.

$$\llbracket \text{CP} \rrbracket (a^\uparrow \sqcup b^\uparrow) = \square \lambda w. [a = \iota y [\text{book}_w(y) \wedge \text{read}_w(j, y)]] \vee [b = \iota y [\text{book}_w(y) \wedge \text{read}_w(j, y)]]$$

(It has to be that the book that John read is Book A or is Book B.)

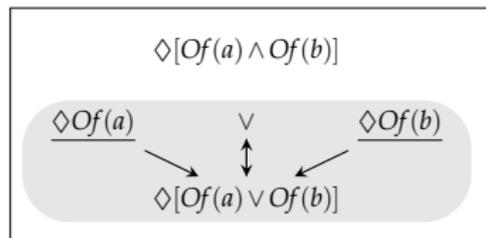
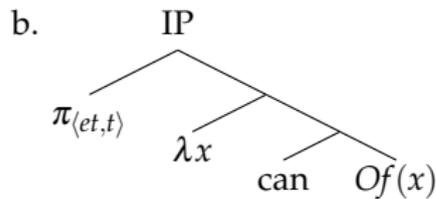
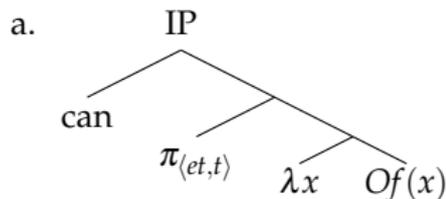
b. #Book A and Book B.

$$\begin{aligned} \llbracket \text{CP} \rrbracket (a^\uparrow \sqcap b^\uparrow) &= \square \lambda w. [a = \iota y [\text{book}_w(y) \wedge \text{read}_w(j, y)]] \wedge [b = \iota y [\text{book}_w(y) \wedge \text{read}_w(j, y)]] \\ &= \perp \text{ (unless } a = b \text{)} \end{aligned}$$

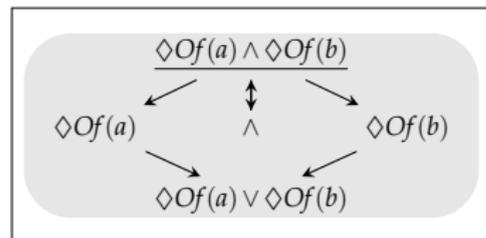
(#It has to be that the book that John read is Book A and is Book B.)

Conjunctive MA arises iff the higher-order trace scopes above the \diamond -modal.

(46) Who can chair the committee? Prof A and Prof B.



$\diamond \gg \pi$: MS



$\pi \gg \diamond$: conjunctive MA

Wide scope uniqueness yield contradiction:

(47) Which professor can chair the committee? # Prof A and Prof B.

$$\begin{aligned} \llbracket \text{CP} \rrbracket (a^\uparrow \sqcap b^\uparrow) = & \lambda w. [a = \iota y [\text{prof}_w(y) \wedge \diamond_w \text{Ochair}(j, y)]] \wedge \\ & [b = \iota y [\text{prof}_w(y) \wedge \diamond_w \text{Ochair}(j, y)]] \end{aligned}$$

Disjunctive MA arises when a covert **DOU**-operator is associated with the higher-order **WH**-trace. The higher-order **WH**-trace can take narrow scope.

Mandarin *dou* triggers **free choice** effect when associated with a pre-verbal disjunction, and forces **exhaustive** readings when associated with a *whP* in a question.

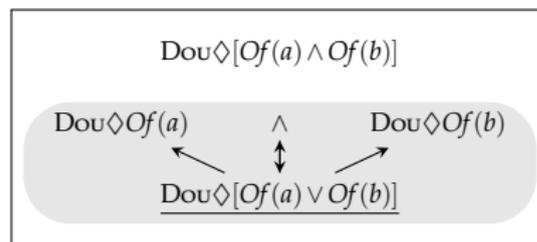
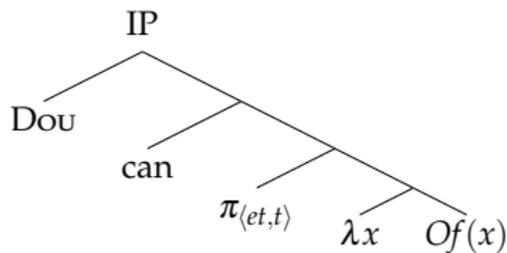
- (48) a. [Yuehan huozhe Mali] **dou** keyi jiao jichu hanyu
John or Mary **DOU** can teach intro Chinese
Intended: 'Both John and Mary can teach Intro Chinese.'
- b. **Dou** [shei] keyi jiao jichu hanyu?
DOU who can teach Intro Chinese
'Who can teach Intro Chinese?' (MA only)

Xiang (To appear): *Dou* is a pre-exh exhaustifier over sub-alternatives.
Sub-alternatives for dis/conjunctions are the dis/con-juncts.

- (49) $\llbracket dou_C \rrbracket = \lambda p \lambda w : \exists q \in \text{SUB}(p, C). p(w) = 1 \wedge \forall q \in \text{SUB}(p, C) [O_C(q)(w) = 0]$

In questions, Dou strengthens disjunctive answers into free choice statements, making the answer space closed under conjunction.

(50) Who can chair the committee? Prof A or Prof B.



With Dou ($\diamond \gg \pi$): disjunctive MA

Narrow scope uniqueness doesn't yield contradiction:

(51) Which professor can chair the committee? Prof A or Prof B.

$$\begin{aligned} \llbracket \text{CP} \rrbracket (a^\uparrow \sqcup b^\uparrow) &= \text{Dou} \diamond \lambda w. \llbracket [a = \iota y [\text{prof}_w(y) \wedge \text{Ochair}_w(j, y)]] \vee \\ &\quad [b = \iota y [\text{prof}_w(y) \wedge \text{Ochair}_w(j, y)]] \rrbracket \\ &= \diamond \lambda w [a = \iota y [\text{prof}_w(y) \wedge \text{Ochair}_w(j, y)] \wedge \\ &\quad \diamond \lambda w [b = \iota y [\text{prof}_w(y) \wedge \text{Ochair}_w(j, y)]] \end{aligned}$$

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